

## Instructions for Epicycloids Geogebra Worksheet

To find parametric equations for an epicycloid, check the “show auxiliary objects” box. Assume

- (a) the radius of the fixed circle is  $a$
- (b) the radius of the rolling circle is  $b$

Let  $\angle AOB = t$  and  $\angle OAP = s$ . Note that because of the rolling, the two orange arcs have the same length, so  $at = bs$ .

Follow the following steps to come up with equations for the  $x$  and  $y$  coordinates of  $P$  in terms of the parameter  $t$ .

1. Express  $\angle OAB$  in terms of  $t$ .
2. Express  $\angle DAP$  in terms of  $s$  and  $t$ .
3.  $x = OC = OB + BC$ . You should be able to express  $OB$  and  $BC$  in terms of  $t$  and/or  $s$  by looking at right triangles  $OBA$  and  $ADP$ . Then since  $at = bs$ , you should be able to express  $x$  in terms of just  $t$  (and of course  $a$  and  $b$ ).
4.  $y = CP = AB - AD$ , so you should be able to express  $y$  in terms of  $t$ ,  $a$ , and  $b$ .

Once you have your equations, enter them into the input boxes and click the “Graph parametric equations” button to verify your answers.