

Pyramid

Construct Pyramids under a given Cube and prove that volume of a pyramid is $\frac{1}{3}$ the volume of cube.

Solution

1. Open a new GeoGebra window
2. Switch to Perspectives \rightarrow 3D Graphing
3. Add Graphics view to the workspace
4. Active the Graphics and create a slider **rotation** running from 0^0 to 90^0 with increment 1^0
 - a. Click on slider tool
 - b. Select angle
 - c. Give name as rotation
 - d. Give minimum value 0^0 , maximum value 90^0 , and increment 1^0
5. Active the Graphics and create a slider **length** running from 1 to 5 with increment 1
 - a. Click on slider tool
 - b. Select number
 - c. Give name as length
 - d. Give minimum value 1, maximum value 5, and increment 1
6. Using Input Box, create three points
 $A=(\text{length},0,0)$, $B=(\text{length},\text{length},0)$ and $C=(0,\text{length},0)$
Hint: to hide the points from Graphics view
 - a. Right click on point
 - b. Click on object properties
 - c. Select advance tab
 - d. In the location option, uncheck Graphics and Graphics 2D
7. Using Input Box, construct a cube as below.
 $\text{cube}=\text{Cube}(A,B,C)$
In the cube, show the name of the eight points A,B,C,D,E,F,G,H
8. Using segment tool, construct a diagonal AG
9. Using midpoint tool, construct the midpoint of AG
And hide the diagonal AG
Rename the midpoint as "center"
10. Using Input Box, construct a pyramid
 $\text{Pyr1}=\text{Pyramid}(A, E, F, B, \text{center})$
11. Using Input Box, construct a line
 $\text{ax1}=\text{Line}(A, B)$
12. Using Input Box, construct a transformation
 $\text{Rot1}=\text{Rotate}(\text{Pyr1}, \text{rotation}, \text{ax1})$
Hide Pyr1
13. Using Input Box, construct a pyramid
 $\text{Pyr2}=\text{Pyramid}(B,C,G,F, \text{center})$
14. Using Input Box, construct a line
 $\text{ax2}=\text{Line}(B,C)$
15. Using Input Box, construct a transformation
 $\text{Rot2}=\text{Rotate}(\text{Pyr2}, \text{rotation}, \text{ax2})$
Hide Pyr2
16. Using Input Box, construct a pyramid
 $\text{Pyr3}=\text{Pyramid}(C,D,H,G, \text{center})$
17. Using Input Box, construct a line
 $\text{ax3}=\text{Line}(C,D)$
18. Using Input Box, construct a transformation
 $\text{Rot3}=\text{Rotate}(\text{Pyr3}, \text{rotation}, \text{ax3})$
Hide Pyr3

19. Using Input Box, construct a pyramid
Pyr4=Pyramid(D,A,E,H, center)
20. Using Input Box, construct a line
ax4=Line(D,A)
21. Using Input Box, construct a transformation
Rot4=Rotate(Pyr4, rotation, ax4)
Hide Pyr4
22. Using Input Box, construct a pyramid
Pyr5=Pyramid(E, F, G, H, center)
23. Using Input Box, construct a line
ax5=Line(E,F)
24. Using Input Box, construct a point
E'=Rotate(E,rotation,ax1)
25. Using Input Box, construct a vector
translate=Vector(E,E')
26. Using Input Box, construct a transformation
Rot5=Translate(Rotate(Pyr5, rotation, ax5),translate)
Hide Pyr5
27. Using Input Box, construct a pyramid
Pyr6=Pyramid(A,B,C,D, center)
28. Now, design the layouts as much as interactive with text and color features